

Course: Geometry Unit: Unit 1 - Foundations of Geometry Grades: 9-10

Stage 1 – Desired Results		
Established Goals	Enduring Understandings/Transfer	
What 21 <sup>st</sup> Century Essentials included in the mission statement will this unit address?      Adaptation and flexibility      Transfer of Learning	Written as a declarative statement, an enduring understanding is a "big idea" that focuses on larger concepts, principles, and processes that go beyond discrete facts or skills. Enduring Understandings are applicable to new situations across content areas and <a href="https://example.com/real-world-new-situation">TRANSFERABLE</a> (the ability to learn in one context and apply to a new situation, particularly outside of the classroom) to the real world.	
<ul><li>Problem-solving</li><li>What content standards will this unit address?</li></ul>	<ol> <li>List the Enduring Understanding(s):</li> <li>a. Geometric relationships and concepts can be modeled and applied in areas such as art, architecture, construction, and engineering.</li> <li>b. Inductive and deductive reasoning skills can be applied through geometric concepts and results in drawing reasonable conclusions.</li> </ol>	
<ul> <li>ELA PA Core State Standards</li> <li>Math PA Core State Standards         CC.2.3.HS.A.3: Verify and apply geometric theorems as they relate to geometric figures.     </li> </ul>	<ul> <li>c. The modeling of geometric concepts apply in all worldly applications.</li> <li>d. Communication of geometric terms in proper notation and definitions is critical for understanding.</li> <li>e. Analyze, verify and justify solutions to problems and explain it to others.</li> <li>f. Communicate mathematical concepts to peers, teachers, and instructional assistants in a safe and encouraging environment.</li> </ul>	
CC.2.3.HS.A.14: Apply geometric concepts to model and solve real world problems.  CC.2.2.HS.C.1 Use the concept and notation of functions to interpret and apply them in terms of their context.  CC.2.3.HS.A.11 Apply coordinate geometry to prove simple geometric theorems algebraically.  PA Content Standards	<ul> <li>4. What do you want students to do with this knowledge or skill beyond this course? What is Transfer? <ul> <li>a. Students will make sense of and persevere in solving complex and novel mathematical problems.</li> <li>b. Students will use effective mathematical reasoning to construct viable arguments and critique the reasoning of others.</li> <li>c. Students will communicate precisely when making mathematical statements and express answers with a degree of precision appropriate for the context of the problem/situation.</li> <li>d. Students will apply mathematical knowledge to analyze and model situations/relationships using multiple representations and appropriate tools in order to make decisions, solve problems, and draw conclusions.</li> <li>e. Students will make use of structure and repeated reasoning to gain a mathematical perspective and formulate generalized problem solving strategies</li> <li>f. Given a word problem, students will solve the word problem using an appropriate strategy or strategies and will share and compare the use of multiple strategies leading to the same answer.</li> </ul> </li> </ul>	

## What thought-provoking questions will foster inquiry, meaning making, and transfer?

5. List the Essential Question(s) that students should ponder, wonder about or explain by the end of this unit: What definitions, equations, notation, and terminology are necessary for success in Geometry?

## Acquisition

#### Students will know...

- 6. What facts should students know and be able to use to gain further knowledge?

  Notation for the building blocks of geometry

  Different line/angle relationships

  Classifications and parts of a polygon

  Classifications and parts of a triangle

  Classifications of special quadrilaterals

  Understanding slope and distance and the application with geometric figures
- 7. What vocabulary should students know and be able to recall?

  Points, lines, planes, line segment, ray, midpoint,
  - Points, lines, planes, line segment, ray, midpoint, endpoints, angle, vertex, protractor, degrees, angle bisector, acute angle, obtuse angle, right angle, reflex angle, linear pair of angles, vertical angles, supplementary angles, complementary angles, adjacent angles, polygon names, consecutive sides, consecutive angles, diagonal, concave/convex polygons, regular/irregular polygons, congruent polygons, acute triangle, obtuse triangle, right triangle (hypotenuse and leg), isosceles triangle (base, base angles, and vertex angle), scalene triangle, regular triangle, trapezoid, isosceles trapezoid, kite, parallelogram, rhombus, rectangle and square, midpoint, distance, slope
- 8. What basic concepts should students know and be able to recall and apply? When given examples and counterexamples,

- 9. What discrete skill and processes should students be able to demonstrate?
  - G.1.2.1.1 Identify and/or use properties of triangles G.1.2.1.2 Identify and/or use properties of auadrilaterals
  - G.1.2.1.3 Identify and/or use properties of isosceles and equilateral triangles.
  - G.1.2.1.4 Identify and/or use properties of regular polygons
  - G.2.1.1.1 Use the Pythagorean Theorem to write and/or solve problems involving right triangles. G.2.1.2.1 Calculate the distance and/or midpoint between two points on a number line or on a coordinate plane
  - G.2.1.2.2 Relate slope to perpendicularity and/or parallelism (limit to linear algebraic equations) G.2.1.2.3 Use slope, distance, and/or midpoint between two points on a coordinate plane to establish properties of a two dimensional shape
  - G.2.2.1.1 Use properties of angles formed by intersecting lines to find the measures of missing angles.
  - G.2.2.1.2 Use properties of angles formed when two parallel lines are cut by a transversal to find the measures of missing angles.

students can construct correct proper definitions.
The basic buildings biocks of geometry: point, line
and plane.
Classify and measure angles and angle pairs
Classify polygons - polygons, triangles and special
quadrilaterals

G.2.2.3.1

Describe how a change in the linear dimension of a figure affects its perimeter, circumference, and area

Stage 2 – Evidence				
NETS for Students	PERFORMANCE TASK(S)—can include transfer tasks and Project-Based Learning			
NETS—National Educational	Examples include but are not limited to:			
Technology Standards; i.e., the	Labs, open-ended essays, voice recordings, videos, presentations, discussion boards, graphic organizers, songs, skits,			
standards for evaluating the skills	dioramas, visual projects (posters, dioramas)			
and knowledge students need to				
learn effectively and live	List the task(s), then explain how the student will demonstrate the transfer of knowledge or skill involved in the task(s)			
productively in an increasingly	(reference Stage 1, Item #4):			
global and digital world.	Student work shared with explanations of work and comparisons to other solutions			
	Investigations using Geometric tools, Sketchpad or Desmos to create their own conjectures			
Critical Thinking	Peer reviewed work			
Creative and Innovation	Quizzes and tests			
	Daily exit tickets			
	Collection/grading of daily homework assignments			
	OTHER SUMMATIVE ASSESSMENTS—can include factual recall			
	Examples include but are not limited to final projects, research papers, quizzes and tests.			
	List the assessments:			
	Mid-Unit Quiz			
	Unit 1 Test			

Stage 3 – Learning Plan			
NETS for Students	Learning Activities	Progress Monitoring/Formative Assessment	
NETS—National Educational	Questions to consider while planning:	How will you monitor students' progress toward	
Technology Standards; i.e., the	Are transfer and acquisition addressed in the learning	acquisition, meaning, and transfer during learning	
standards for evaluating the skills	plan?	activities?	
and knowledge students need to	Does the learning plan reflect principles of learning and	Daily assessments, teacher observation of student in-	
learn effectively and live	best practices?	class performance, teacher observation of student	
productively in an increasingly	<ul> <li>Is there tight alignment with Stages 1 and 2?</li> </ul>	presentations.	
global and digital world.	Is the plan likely to be engaging and effective for all	What are potential rough spots and student	
	students?	misunderstandings?	

Communication and Collaboration			Appropriately using notation on geometric figures:
Creative and Innovation			segments, points, lines, quadrilaterals, midpoints,
Research and Information Fluency			angle bisectors
Critical Thinking			
			<ul> <li>How will students get the feedback they need?</li> </ul>
			Graded homework assessments, immediate feedback
			during in-class assignments, mid-chapter quiz, peer
			feedback and discussion
	List planned activities	List resources required	FORMATIVE ASSESSMENTS—any non-graded, diagnostic
	(examples include but are not	(examples include but are not	assessment administered prior to or during a unit that
	limited to: experiments,	limited to: laptops, iPads,	reflects prior knowledge, skill levels, and potential
	guided reading, worksheets,	websites, digital cameras,	misconceptions.
	discussions, note-taking,	magazines, Blackboard,	
	research, games):	textbooks, novels, primary	Examples include but are not limited to: Pre-tests, clickers
		source documents, other non-	(CPS), mini whiteboards, entrance and exit tickets, CDTs,
		fiction text, lab equipment,	DIBELS, Aimsweb
	Definition Pictionary	maps, translator, calculators)	
	Definition Presentations	Textbook, notebook, ruler,	Whiteboards
	Word Wall	protractor, compass	Warm up problems
	Duplicating angles and line	straightedge, white boards,	
	segments	and calculators	
	Note-taking		
	In-Class Assignments		



Course: Geometry Unit: Unit 2 - Forms of Reasoning Grades: 9-10

Stage 1 – Desired Results		
Established Goals	Enduring Understandings/Transfer	
What 21 <sup>st</sup> Century Essentials included in the mission statement will this unit address?      Adaptation and flexibility      Transfer of Learning      Problem solving	Written as a declarative statement, an enduring understanding is a "big idea" that focuses on larger concepts, principles, and processes that go beyond discrete facts or skills. Enduring Understandings are applicable to new situations across content areas and <a href="https://example.com/">TRANSFERABLE</a> (the ability to learn in one context and apply to a new situation, particularly outside of the classroom) to the real world.	
<ul> <li>Problem-solving</li> <li>What content standards will this unit address?</li> <li>ELA PA Core State Standards</li> <li>Math PA Core State Standards CC.2.3.HS.A.3: Verify and apply</li> </ul>	<ul> <li>3. List the Enduring Understanding(s):</li> <li>a. Geometric relationships and concepts can be modeled and applied in areas such as art, architecture, construction, and engineering.</li> <li>b. Inductive and deductive reasoning skills can be applied through geometric concepts and results in drawing reasonable conclusions.</li> <li>c. The modeling of geometric concepts apply in all worldly applications.</li> <li>d. Communication of geometric terms in proper notation and definitions is critical for understanding.</li> <li>e. Students analyze, verify and justify their solutions to problems and can explain it to others.</li> <li>f. Communicate mathematical concepts to peers, teachers, and instructional assistants in a safe and</li> </ul>	
geometric theorems as they relate to geometric figures.  • PA Content Standards	<ul> <li>4. What do you want students to do with this knowledge or skill beyond this course? What is Transfer? <ul> <li>a. Students will make sense of and persevere in solving complex and novel mathematical problems.</li> <li>b. Students will use effective mathematical reasoning to construct viable arguments and critique the reasoning of others.</li> <li>c. Students will communicate precisely when making mathematical statements and express answers with a degree of precision appropriate for the context of the problem/situation.</li> <li>d. Students will apply mathematical knowledge to analyze and model situations/relationships using multiple representations and appropriate tools in order to make decisions, solve problems, and draw conclusions.</li> <li>e. Students will make use of structure and repeated reasoning to gain a mathematical perspective and formulate generalized problem solving strategies</li> <li>f. Given a word problem, students will solve the word problem using an appropriate strategy or strategies and will share and compare the use of multiple strategies leading to the same answer.</li> </ul> </li> </ul>	

## What thought-provoking questions will foster inquiry, meaning making, and transfer?

5. List the Essential Question(s) that students should ponder, wonder about or explain by the end of this unit: What is the difference between inductive and deductive reasoning and how can each help us solve real-world problems?

### **Acquisition**

#### Students will know...

- 6. What facts should students know and be able to use to gain further knowledge?

  Basic algebraic concepts such as variables and solving a two step equation, factoring, etc.
- 7. What vocabulary should students know and be able to recall?

  Inductive reasoning, deductive reasoning, nth term, conditional, inverse, converse, contrapositive, biconditional, two column proof, direct proofs, indirect proofs, conclusion, conjecture, counterexample, equivalent statements, negation, theorem, hypothesis
- 8. What basic concepts should students know and be able to recall and apply?

  Difference between inductive and deductive reasoning

  Difference between a conditional statement, it's converse, it's inverse, it's biconditional, and it's contrapositive

  How to determine the nth term of a sequence How to write a two column proof

  How to make a proper conjecture using inductive reasoning

- 9. What discrete skill and processes should students be able to demonstrate?
  - G.1.2.1.1 Identify and/or use properties of triangles G.1.2.1.2 Identify and/or use properties of quadrilaterals
  - G.1.2.1.3 Identify and/or use properties of isosceles and equilateral triangles.
  - G.1.2.1.4 Identify and/or use properties of regular polygons
  - G.2.2.1.1 Use properties of angles formed by intersecting lines to find the measures of missing angles.
  - G.2.2.1.2 Use properties of angles formed when two parallel lines are cut by a transversal to find the measures of missing angles.

Stage 2 – Evidence				
NETS for Students	ETS for Students PERFORMANCE TASK(S)—can include transfer tasks and Project-Based Learning			
NETS—National Educational	Examples include but are not limited to:			
Technology Standards; i.e., the	Labs, open-ended essays, voice recordings, videos, presentations, discussion boards, graphic organizers, songs, skits,			
standards for evaluating the skills	dioramas, visual projects (posters, dioramas)			
and knowledge students need to				
learn effectively and live	List the task(s), then explain how the student will demonstrate the transfer of knowledge or skill involved in the task(s)			
productively in an increasingly	(reference Stage 1, Item #4):			
global and digital world.				
	Student work shared with explanations of work and comparisons to other solutions			
Critical Thinking	Investigations using Geometric tools, Sketchpad or Desmos to create their own conjectures			
Creative and Innovation	Peer reviewed work			
	Quizzes and tests			
	Daily exit tickets			
	Collection/grading of daily homework assignments			
	OTHER SUMMATIVE ASSESSMENTS—can include factual recall			
	Examples include but are not limited to final projects, research papers, quizzes and tests.			
	List the assessments:			
	Basic Reasoning/nth Term Quiz			
	Unit 2 Exam			

Stage 3 – Learning Plan			
NETS for Students	Learning Activities	Progress Monitoring/Formative Assessment	
NETS—National Educational	Questions to consider while planning:	How will you monitor students' progress toward	
Technology Standards; i.e., the	Are transfer and acquisition addressed in the learning	acquisition, meaning, and transfer during learning	
standards for evaluating the skills	plan?	activities?	
and knowledge students need to	Does the learning plan reflect principles of learning and	Daily assessments, teacher observation of student in-	
learn effectively and live	best practices?	class performance, teacher observation of student	
productively in an increasingly	<ul> <li>Is there tight alignment with Stages 1 and 2?</li> </ul>	presentations.	
global and digital world.	Is the plan likely to be engaging and effective for all	What are potential rough spots and student	
	students?	misunderstandings?	
Communication and Collaboration		Finding the nth term	
Creative and Innovation		Students' first experience with proofs	
Research and Information Fluency			
Critical Thinking		<ul> <li>How will students get the feedback they need?</li> </ul>	
		Graded homework assessments, immediate feedback	
		during in-class assignments, mid-chapter quiz, peer	

			feedback and discussion
L	List planned activities	List resources required	FORMATIVE ASSESSMENTS—any non-graded, diagnostic
	(examples include but are not	(examples include but are not	assessment administered prior to or during a unit that
	limited to: experiments,	limited to: laptops, iPads,	reflects prior knowledge, skill levels, and potential
g	guided reading, worksheets,	websites, digital cameras,	misconceptions.
	discussions, note-taking,	magazines, Blackboard,	
r	research, games):	textbooks, novels, primary	Examples include but are not limited to: Pre-tests, clickers
		source documents, other non-	(CPS), mini whiteboards, entrance and exit tickets, CDTs,
		fiction text, lab equipment,	DIBELS, Aimsweb
P	Proof Puzzle Activity	maps, translator, calculators)	
	Definition Presentations	Textbook, notebook, ruler,	Whiteboards
	Note-taking	protractor, compass	Warm up problems
l li	In-Class Assignments	straightedge, white boards,	
		and calculators	



Course: Geometry Unit: Unit 3 - Triangle Congruence Grades: 9-10

Stage 1 – Desired Results		
Established Goals	Enduring Understandings/Transfer	
1. What 21 <sup>st</sup> Century Essentials included in the mission statement will this unit address?	Written as a declarative statement, an enduring understanding is a "big idea" that focuses on larger concepts, principles, and processes that go beyond discrete facts or skills. Enduring Understandings are applicable to new situations across content areas and <a href="https://example.com/reastandings">TRANSFERABLE</a> (the ability to learn in one context and apply to a new situation,	
Adaptation and flexibility Transfer of Learning	particularly outside of the classroom) to the real world.	
Problem-solving Effective Communication Skills	3. List the Enduring Understanding(s):  a. Geometric relationships and concepts can be modeled and applied in areas such as art, architecture, construction, and engineering.	
2. What content standards will this unit address?	<ul> <li>b. Inductive and deductive reasoning skills can be applied through geometric concepts and results in drawing reasonable conclusions.</li> <li>c. The modeling of geometric concepts apply in all worldly applications.</li> </ul>	
• ELA PA Core State Standards	d. Communication of geometric terms in proper notation and definitions is critical for understanding.  e. Students analyze, verify and justify their solutions to problems and can explain it to others.	
<ul> <li>Math PA Core State Standards         CC.2.3.HS.A.3: Verify and apply             geometric theorems as they relate to             geometric figures.     </li> </ul>	f. Communicate mathematical concepts to peers, teachers, and instructional assistants in a safe and encouraging environment.	
CC.2.3.HS.A.14: Apply geometric concepts to model and solve real world problems. CC.2.3.HS.A.2 Apply rigid transformation	<ul> <li>4. What do you want students to do with this knowledge or skill beyond this course? What is Transfer?         <ul> <li>a. Students will make sense of and persevere in solving complex and novel mathematical problems.</li> <li>b. Students will use effective mathematical reasoning to construct viable arguments and critique the reasoning of others.</li> </ul> </li> </ul>	
to determine and explain congruence CC.2.3.HS.A.4 Apply the concept of congruence to create geometric constructions.	<ul> <li>c. Students will communicate precisely when making mathematical statements and express answers with a degree of precision appropriate for the context of the problem/situation.</li> <li>d. Students will apply mathematical knowledge to analyze and model situations/relationships using multiple representations and appropriate tools in order to make decisions, solve problems, and draw conclusions.</li> <li>e. Students will make use of structure and repeated reasoning to gain a mathematical perspective and</li> </ul>	
PA Content Standards	formulate generalized problem solving strategies  f. Given a word problem, students will solve the word problem using an appropriate strategy or strategies  and will share and compare the use of multiple strategies leading to the same answer.	

Essential (	Questions
What thought-provoking questions will foster inquiry, r	meaning-making, and transfer?
5. List the Essential Question(s) that students should por How do the relationships of congruence help us solve	• • • • • • • • • • • • • • • • • • • •
Acqui	sition
Students will know	Students will be skilled at (be able to do)
6. What facts should students know and be able to use to gain further knowledge?  Proper Geometry notation  Classification of triangles by sides and angles	9. What discrete skill and processes should students be able to demonstrate?
Deductive Reasoning skills and proof	G.1.2.1.1 Identify and/or use properties of triangles G.1.2.1.3 Identify and/or use properties of isosceles
7. What vocabulary should students know and be able to recall?	and equilateral triangles.
acute, obtuse, right, equiangular, scalene, equilateral, isosceles triangles, base, legs, hypotenuse of triangles, base, base angle, vertex,	G.1.3.1.1 Identify and/or use properties of congruence.
vertex angle, interior and exterior angles, remote interior angles, corresponging angles, corresponding sides, included side and angle, congruence, CPCTC	G.1.3.2.1 Write, analyze, complete or identify formal proofs.
8. What basic concepts should students know and be	

Stage 2 – Evidence		
NETS for Students	PERFORMANCE TASK(S)—can include transfer tasks and Project-Based Learning	
NETS—National Educational	Examples include but are not limited to:	
Technology Standards; i.e., the	Labs, open-ended essays, voice recordings, videos, presentations, discussion boards, graphic organizers, songs, skits,	
standards for evaluating the skills	dioramas, visual projects (posters, dioramas)	
and knowledge students need to		

able to recall and apply?

relationships

Angle Relationships in Triangles

Classifying Triangles by sides and angles

Congurence in Triangles and proving these

Isosceles and Equilateral Triangle Relationships

learn effectively and live
productively in an increasingly
global and digital world.

Critical Thinking Creative and Innovation Communication and Collaboration Technology Operations List the task(s), then explain how the student will demonstrate the transfer of knowledge or skill involved in the task(s) (reference Stage 1, Item #4):

Student work shared with explanations of work

Investigations using Geometric tools, Sketchpad or Desmos to create their own conjectures

Quizzes and tests

Daily exit tickets

Practice proofs

Questions regarding daily homework assignments

## OTHER SUMMATIVE ASSESSMENTS—can include factual recall

Examples include but are not limited to final projects, research papers, quizzes and tests.

List the assessments:

Mid-Unit Quiz

End of Unit Quiz

Proof Test

Stage 3 – Learning Plan		
NETS for Students	Learning Activities	Progress Monitoring/Formative Assessment
NETS—National Educational Technology Standards; i.e., the standards for evaluating the skills and knowledge students need to learn effectively and live productively in an increasingly global and digital world.  Communication and Collaboration Creative and Innovation Research and Information Fluency Critical Thinking	<ul> <li>Questions to consider while planning:</li> <li>Are transfer and acquisition addressed in the learning plan?</li> <li>Does the learning plan reflect principles of learning and best practices?</li> <li>Is there tight alignment with Stages 1 and 2?</li> <li>Is the plan likely to be engaging and effective for all students?</li> </ul>	<ul> <li>How will you monitor students' progress toward acquisition, meaning, and transfer during learning activities?         Daily assessments, teacher observation of student inclass performance, teacher observation of student presentations.     </li> <li>What are potential rough spots and student misunderstandings?         Students will have difficulty completing proofs in both equality or congruence situations.     </li> <li>How will students get the feedback they need?         Homework assessments, immediate feedback during in-class assignments, mid-chapter quiz, peer feedback and discussion     </li> </ul>

List planned activities	List resources required	FORMATIVE ASSESSMENTS—any non-graded, diagnostic
(examples include but are no	(examples include but are not	assessment administered prior to or during a unit that
limited to: experiments,	limited to: laptops, iPads,	reflects prior knowledge, skill levels, and potential
guided reading, worksheets,	websites, digital cameras,	misconceptions.
discussions, note-taking,	magazines, Blackboard,	
research, games):	textbooks, novels, primary	Examples include but are not limited to: Pre-tests, clickers
	source documents, other non-	(CPS), mini whiteboards, entrance and exit tickets, CDTs,
	fiction text, lab equipment,	DIBELS, Aimsweb
Practice Proofs	maps, translator, calculators)	
Peer and Group Proof	Textbook, notebook, ruler,	Whiteboards
practice	protractor, compass	Warm up problems
Note-taking	straightedge, white boards,	Lesson Quizzes
In-Class Assignments	and calculators, sketchpad	



Course: Geometry Unit: Unit 4 - Triangle Similarity Grades: 9-10

Stage 1 – Desired Results		
Established Goals	Enduring Understandings/Transfer	
1. What 21 <sup>st</sup> Century Essentials included in	Written as a declarative statement, an enduring understanding is a "big idea" that focuses on larger concepts,	
the mission statement will this unit	principles, and processes that go beyond discrete facts or skills. Enduring Understandings are applicable to	
address?	new situations across content areas and TRANSFERABLE (the ability to learn in one context and apply to a new situation,	
Adaptation and flexibility	particularly outside of the classroom) to the real world.	
Transfer of Learning		
Problem-solving	3. List the Enduring Understanding(s):	
Effective Communication Skills	a. Geometric relationships and concepts can be modeled and applied in areas such as art, architecture,	
	construction, and engineering.	
2. What content standards will this unit	b. Inductive and deductive reasoning skills can be applied through geometric concepts and results in drawing	
address?	reasonable conclusions. c. The modeling of geometric concepts apply in all worldly applications.	
Please access the appropriate standards and	d. Communication of geometric terms in proper notation and definitions is critical for understanding.	
copy/paste in the gray region	e. Students analyze, verify and justify their solutions to problems and can explain it to others.	
copy, paste in the gray region	f. Communicate mathematical concepts to peers, teachers, and instructional assistants in a safe and	
ELA PA Core State Standards	encouraging environment.	
Math PA Core State Standards		
CC.2.3.HS.A.3: Verify and apply	4. What do you want students to do with this knowledge or skill beyond this course? What is Transfer?	
geometric theorems as they relate to	a. Students will make sense of and persevere in solving complex and novel mathematical problems.	
geometric figures.	b. Students will use effective mathematical reasoning to construct viable arguments and critique the	
CC.2.3.HS.A.14: Apply geometric	reasoning of others.	
concepts to model and solve real world	c. Students will communicate precisely when making mathematical statements and express answers with a	
problems.	degree of precision appropriate for the context of the problem/situation.	
CC.2.3.HS.A.5 Create justifications based	d. Students will apply mathematical knowledge to analyze and model situations/relationships using multiple	
on transformations to establish	representations and appropriate tools in order to make decisions, solve problems, and draw conclusions.	
similarity of plane figures.	e. Students will make use of structure and repeated reasoning to gain a mathematical perspective and	
***************************************	formulate generalized problem solving strategies	
**CC.2.3.HS.A.9 Extend the concept of	f. Given a word problem, students will solve the word problem using an appropriate strategy or strategies and will share and compare the use of multiple strategies leading to the same answer.	
similarity to determine arc lengths and	und win share and compare the use of maniple strategies leading to the same unswer.	

areas of sectors of circles.

CC.2.3.8.A.2 Understand and apply congruence, similarity and geometric transformations using various tools. CC.2.3.HS.A.2 Apply rigid transformation to determine and explain congruence CC.2.3.HS.A.6 Verify and apply theormens involving similarity as they relate to plane figures. CC.2.3.HS.A.1 Use geometric figures and their properties to represent transformations in the plane.

PA Content Standards

#### **Essential Questions**

## What thought-provoking questions will foster inquiry, meaning-making, and transfer?

5. List the Essential Question(s) that students should ponder, wonder about or explain by the end of this unit: How do the relationships of angles and segments that intersect with circles help us solve real-world problems?

## Acquisition

#### Students will know...

- 6. What facts should students know and be able to use to gain further knowledge?

  Proper Geometry notation

  Classification of angles

  Deductive Reasoning skills and proof
- 7. What vocabulary should students know and be able to recall?

  acute, obtuse, right, scalene, equilateral, isosceles triangles, base, legs, hypotenuse of triangles, base, vertex, interior and exterior angles, remote interior angles, corresponging angles, corresponding sides, included side and angle, corresponding angles of similar triangles are congruent, corresponding sides of similar triangles are proportional, dialation, scale factor, scale drawing, scale, similar, similarity ratio
- 8. What basic concepts should students know and be able to recall and apply?

  Transformations in the coordinate plane (dialations)
  Ratios in Similar Polygons
  Triangle Similarity: AA, SSS, SAS
  Properties and Relationships in Similar Triangles and using them to solve problems
  Similarity in Triangles and proving these relationships

- 9. What discrete skill and processes should students be able to demonstrate?
  - G.1.2.1.1 Identify and/or use properties of triangles G.1.2.1.3 Identify and/or use properties of isosceles and equilateral triangles.
  - G.1.3.1.1 Identify and/or use properties of congruent and similar polygons or solids. G.1.3.1.2 Identify and/or use proportional relationships in similar figures.
  - G.1.3.2.1 Write, analyze, complete, or identify formal proofs (e.g., direct and/or indirect proofs/proofs by contradiction)

Stage 2 – Evidence			
NETS for Students	PERFORMANCE TASK(S)—can include transfer tasks and Project-Based Learning		
NETS—National Educational	Examples include but are not limited to:		
Technology Standards; i.e., the	Labs, open-ended essays, voice recordings, videos, presentations, discussion boards, graphic organizers, songs, skits,		
standards for evaluating the skills	dioramas, visual projects (posters, dioramas)		
and knowledge students need to			
learn effectively and live	List the task(s), then explain how the student will demonstrate the transfer of knowledge or skill involved in the task(s)		
productively in an increasingly	(reference Stage 1, Item #4):		
global and digital world.	Student work shared with explanations of work		
	Investigations using Geometric tools, Sketchpad or Desmos to create their own conjectures		
Critical Thinking	Quizzes and tests		
Creative and Innovation	Daily exit tickets		
Communication and Collaboration	Practice proofs		
Technology Operations	Questions regarding daily homework assignments		
	Scale Drawing		
	OTHER SUMMATIVE ASSESSMENTS—can include factual recall		
	Examples include but are not limited to final projects, research papers, quizzes and tests.		
	List the assessments:		
	Mid-Unit Quiz		
	End of Unit Quiz		
	Proof Test		

Stage 3 – Learning Plan		
NETS for Students	Learning Activities	Progress Monitoring/Formative Assessment
NETS—National Educational	Questions to consider while planning:	How will you monitor students' progress toward
Technology Standards; i.e., the standards for evaluating the skills	Are transfer and acquisition addressed in the learning	acquisition, meaning, and transfer during learning activities?
and knowledge students need to learn effectively and live productively in an increasingly global and digital world.	<ul> <li>plan?</li> <li>Does the learning plan reflect principles of learning and best practices?</li> <li>Is there tight alignment with Stages 1 and 2?</li> <li>Is the plan likely to be engaging and effective for all</li> </ul>	Daily assessments, teacher observation of student inclass performance, teacher observation of student presentations.  • What are potential rough spots and student
Communication and Collaboration Creative and Innovation Research and Information Fluency	students?	misunderstandings? Students will have difficulty completing proofs in similarity situations.
Critical Thinking		How will students get the feedback they need?     Homework assessments, immediate feedback during in-class assignments, mid-chapter quiz, peer feedback

		and discussion
List planned activities	List resources required	FORMATIVE ASSESSMENTS—any non-graded, diagnostic
(examples include but are not	(examples include but are not	assessment administered prior to or during a unit that
limited to: experiments,	limited to: laptops, iPads,	reflects prior knowledge, skill levels, and potential
guided reading, worksheets,	websites, digital cameras,	misconceptions.
discussions, note-taking,	magazines, Blackboard,	
research, games):	textbooks, novels, primary	Examples include but are not limited to: Pre-tests, clickers
	source documents, other non-	(CPS), mini whiteboards, entrance and exit tickets, CDTs,
	fiction text, lab equipment,	DIBELS, Aimsweb
Practice Proofs	maps, translator, calculators)	
Peer and Group Proof	Textbook, notebook, ruler,	Whiteboards
practice	protractor, compass	Warm up problems
Note-taking	straightedge, white boards,	Lesson Quizzes
In-Class Assignments	and calculators, sketchpad	



Date: October, 2016

Course: Geometry Unit: Unit 5 - Quadrilaterals and Polygons Grades: 9-10

Teacher Team: Greenawald, Dottery, Skrapits, Everett

Stage 1 – Desired Results		
Established Goals	Enduring Understandings/Transfer	
What 21 <sup>st</sup> Century Essentials included in	Written as a declarative statement, an enduring understanding is a "big idea" that focuses on larger concepts,	
the mission statement will this unit	principles, and processes that go beyond discrete facts or skills. Enduring Understandings are applicable to	
address?	new situations across content areas and TRANSFERABLE (the ability to learn in one context and apply to a new situation,	
Adaptation and flexibility	particularly outside of the classroom) to the real world.	
Transfer of Learning		
Problem-solving	3. List the Enduring Understanding(s):	
Effective Communication Skills	a. Geometric relationships and concepts can be modeled and applied in areas such as art, architecture,	
	construction, and engineering.	
2. What content standards will this unit	b. Inductive and deductive reasoning skills can be applied through geometric concepts and results in drawing	
address?	reasonable conclusions.	
	c. The modeling of geometric concepts apply in all worldly applications.	
<ul> <li>ELA PA Core State Standards</li> </ul>	d. Communication of geometric terms in proper notation and definitions is critical for understanding.	
	e. Students analyze, verify and justify their solutions to problems and can explain it to others.	
Math PA Core State Standards	f. Communicate mathematical concepts to peers, teachers, and instructional assistants in a safe and encouraging environment.	
CC.2.3.HS.A.3: Verify and apply		
geometric theorems as they relate to		
geometric figures.	4. What do you want students to do with this knowledge or skill beyond this course? What is Transfer?	
CC.2.3.HS.A.11 Apply coordinate	a. Students will make sense of and persevere in solving complex and novel mathematical problems.	
geometry to prove simple geometric theorems algebraically.	<ul> <li>Students will use effective mathematical reasoning to construct viable arguments and critique the reasoning of others.</li> </ul>	
CC.2.3.HS.A.14: Apply geometric	c. Students will communicate precisely when making mathematical statements and express answers with a	
concepts to model and solve real world	degree of precision appropriate for the context of the problem/situation.	
problems.	d. Students will apply mathematical knowledge to analyze and model situations/relationships using multiple	
CC.2.3.HS.A.2 Apply rigid transformation	representations and appropriate tools in order to make decisions, solve problems, and draw conclusions.	
to determine and explain congruence	e. Students will make use of structure and repeated reasoning to gain a mathematical perspective and	
	formulate generalized problem solving strategies	
• PA Content Standards	f. Given a word problem, students will solve the word problem using an appropriate strategy or strategies	
	and will share and compare the use of multiple strategies leading to the same answer.	
1		

## What thought-provoking questions will foster inquiry, meaning-making, and transfer?

5. List the Essential Question(s) that students should ponder, wonder about or explain by the end of this unit: How do the relationships of quadrilaterals/polygons help us solve real-world problems?

### Acquisition

### Students will know...

6. What facts should students know and be able to use to gain further knowledge?

Proper Geometry notation
Basic geometry defintions
Classification of angles and sides
Writing linear equations
Determine missing angles: vertical, linear pairs,
alternate interior/exterior, and cooresponding
Deductive Reasoning skills and proof

- 7. What vocabulary should students know and be able to recall?

  polygon, n-gon, exterior/interior angle,
  regular/irregular, base, leg, base angle, vertex, side,
  concave, convex, diagonal, isosceles, parallelogram,
  kite, non vertex angles, midsegment, rectangle,
  rhombus, square, trapezoid
- 8. What basic concepts should students know and be able to recall and apply?

  Classify polygons based on sides and angles

  Find measures of interior and exterior angles of polygons

  Properties and Conditions of Parallelograms and special parallelograms, kites and trapezoids

- 9. What discrete skill and processes should students be able to demonstrate?
  - G.1.2.1.2 Identify and/or use properties of quadrilaterals
    G.1.2.1.4 Identify and/or use properties of regular polygons.
  - G.1.3.1.1 Identify and/or use properties of congruence.
  - G.2.1.2.2 Relate slope to perpendicularity and/or parallelism (limit to linear algebraic equations)
    G.2.1.2.3 Use slope, distance, and/or midpoint between two points on a coordinate plane to establish properties of a two dimensional shape G.2.2.1.1 Use properties of angles formed by intersecting lines to find the measures of missing angles.
  - G.2.2.1.2 Use properties of angles formed when two parallel lines are cut by a transversal

Stage 2 – Evidence			
NETS for Students	PERFORMANCE TASK(S)—can include transfer tasks and Project-Based Learning		
NETS—National Educational	Examples include but are not limited to:		
Technology Standards; i.e., the	Labs, open-ended essays, voice recordings, videos, presentations, discussion boards, graphic organizers, songs, skits,		
standards for evaluating the skills	dioramas, visual projects (posters, dioramas)		
and knowledge students need to			
learn effectively and live	List the task(s), then explain how the student will demonstrate the transfer of knowledge or skill involved in the task(s)		
productively in an increasingly	(reference Stage 1, Item #4):		
global and digital world.	Student work shared with explanations of work		
	Investigations using Geometric tools, Sketchpad or Desmos to create their own conjectures		
Critical Thinking	Quizzes and tests		
Creative and Innovation	Exit tickets		
Communication and Collaboration	Questions regarding daily homework assignments		
Technology Operations	OTHER SUMMATIVE ASSESSMENTS—can include factual recall		
	Examples include but are not limited to final projects, research papers, quizzes and tests.		
	List the assessments:		
	Mid-Unit Quiz		
	End of Unit Test		

Stage 3 – Learning Plan		
NETS for Students	Learning Activities	Progress Monitoring/Formative Assessment
NETS—National Educational Technology Standards; i.e., the standards for evaluating the skills and knowledge students need to learn effectively and live productively in an increasingly global and digital world.  Communication and Collaboration Creative and Innovation Research and Information Fluency Critical Thinking	<ul> <li>Questions to consider while planning:</li> <li>Are transfer and acquisition addressed in the learning plan?</li> <li>Does the learning plan reflect principles of learning and best practices?</li> <li>Is there tight alignment with Stages 1 and 2?</li> <li>Is the plan likely to be engaging and effective for all students?</li> </ul>	<ul> <li>How will you monitor students' progress toward acquisition, meaning, and transfer during learning activities?         Daily assessments, teacher observation of student inclass performance, teacher observation of student presentations.     </li> <li>What are potential rough spots and student misunderstandings?         Solving for unknown amount of sides given the interior angle sum. Using algebra to find missing meausures in polygons.     </li> <li>How will students get the feedback they need?         Homework assessments, immediate feedback during in-class assignments, mid-chapter quiz, peer feedback     </li> </ul>

		and discussion
List planned activities	List resources required	FORMATIVE ASSESSMENTS—any non-graded, diagnostic
(examples include but are not	(examples include but are not	assessment administered prior to or during a unit that
limited to: experiments,	limited to: laptops, iPads,	reflects prior knowledge, skill levels, and potential
guided reading, worksheets,	websites, digital cameras,	misconceptions.
discussions, note-taking,	magazines, Blackboard,	
research, games):	textbooks, novels, primary	Examples include but are not limited to: Pre-tests, clickers
	source documents, other non-	(CPS), mini whiteboards, entrance and exit tickets, CDTs,
	fiction text, lab equipment,	DIBELS, Aimsweb
Experiments	maps, translator, calculators)	
Study Guide Development	Textbook, notebook, ruler,	Whiteboards
Note-taking	protractor, compass	Warm up problems
In-Class Assignments	straightedge, white boards,	Lesson Quizzes
	and calculators, sketchpad	



Course: Geometry Unit: Unit 6 - Polygon Similarity Grades: 8-11

Stage 1 – Desired Results		
Established Goals	Enduring Understandings/Transfer	
1. What 21 <sup>st</sup> Century Essentials included in	Written as a declarative statement, an enduring understanding is a "big idea" that focuses on larger concepts,	
the mission statement will this unit	principles, and processes that go beyond discrete facts or skills. Enduring Understandings are applicable to	
address?	new situations across content areas and TRANSFERABLE (the ability to learn in one context and apply to a new situation,	
Adaptation and flexibility	particularly outside of the classroom) to the real world.	
Transfer of Learning		
Problem-solving	3. List the Enduring Understanding(s):	
Effective Communication Skills	a. Geometric relationships and concepts can be modeled and applied in areas such as art, architecture, construction, and engineering.	
2. What content standards will this unit address?	b. Inductive and deductive reasoning skills can be applied through geometric concepts and results in drawing reasonable conclusions.	
	c. The modeling of geometric concepts apply in all worldly applications.	
• ELA PA Core State Standards	d. Communication of geometric terms in proper notation and definitions is critical for understanding.	
	e. Students analyze, verify and justify their solutions to problems and can explain it to others.	
<ul> <li>Math PA Core State Standards</li> </ul>	f. Communicate mathematical concepts to peers, teachers, and instructional assistants in a safe and	
CC.2.3.HS.A.1 Use geometric figures and	encouraging environment.	
their properties to represent		
transformations in the plane.		
CC.2.3.HS.A.3: Verify and apply	4. What do you want students to do with this knowledge or skill beyond this course? What is Transfer?	
geometric theorems as they relate to	a. Students will make sense of and persevere in solving complex and novel mathematical problems.	
geometric figures.	b. Students will use effective mathematical reasoning to construct viable arguments and critique the	
CC.2.3.HS.A.14: Apply geometric	reasoning of others.	
concepts to model and solve real world problems.	c. Students will communicate precisely when making mathematical statements and express answers with a degree of precision appropriate for the context of the problem/situation.	
CC.2.3.HS.A.5 Create justifications based	d. Students will apply mathematical knowledge to analyze and model situations/relationships using multiple	
on transformations to establish	representations and appropriate tools in order to make decisions, solve problems, and draw conclusions.	
similarity of plane figures.	e. Students will make use of structure and repeated reasoning to gain a mathematical perspective and	
CC.2.3.HS.A.6 Verify and apply theorems	formulate generalized problem solving strategies	
involving similarity as they relate to	f. Given a word problem, students will solve the word problem using an appropriate strategy or strategies	
plane figures.	and will share and compare the use of multiple strategies leading to the same answer.	
Platic figures.		

CC.2.3.HS.A.8 Apply geometric theorems to verify properties of circles. CC.2.3.HS.A.13 Analyze relationships between two - dimensional and three - dimensional objects.

CC.2.3.8.A.1 Apply the concepts of volume of cylinders, cones, and spheres to solve real - world and mathematical problems.

CC.2.3.8.A.2 Understand and apply congruence, similarity, and geometric transformations using various tools. CC.2.3.HS.A.2 Apply rigid transformation to determine and explain congruence

PA Content Standards

#### **Essential Questions**

## What thought-provoking questions will foster inquiry, meaning-making, and transfer?

5. List the Essential Question(s) that students should ponder, wonder about or explain by the end of this unit: How do similar figures help us solve real-world problems?

### Acquisition

### Students will know...

- 6. What facts should students know and be able to use to gain further knowledge?

  Proper Geometry notation

  Basic geometry definitions

  Solving and setting up proportions

  Distributive property

  Classification of angles

  Deductive Reasoning skills and proof
- 7. What vocabulary should students know and be able to recall?

  acute, obtuse, right, scalene, equilateral, isosceles triangles, base, legs, hypotenuse of triangles, base, vertex, interior and exterior angles, remote interior angles, corresponging angles, corresponding sides, included side and angle, CPCTC, AA, SSS, SAS, angle bisectors, medians, altitudes, midsegment, parallel lines, polygons
- 8. What basic concepts should students know and be able to recall and apply?

  Transformations in the coordinate plane
  Classifying Triangles by sides and angles
  Angle Relationships in Triangles
  Congurence in Triangles and proving these relationships
  Isosceles and Equilateral Triangle Relationships

- 9. What discrete skill and processes should students be able to demonstrate?
  - G.1.2.1.1 Identify and/or use properties of triangles
  - G.1.2.1.2 Identify and/or use properties of quadrilaterals.
  - G.1.2.1.3 Identify and/or use properties of isosceles and equilateral triangles.
  - G.1.3.1.1 Identify and/or use properties of congruent and similar polygons or solids.
  - G.1.3.1.2 Identify and/or use proportional relationships in similar figures.
  - G.1.3.2.1 Write, analyze, complete, or identify formal proofs (e.g., direct and/or indirect proofs/proofs by contradiction).

Stage 2 – Evidence		
NETS for Students	PERFORMANCE TASK(S)—can include transfer tasks and Project-Based Learning	
NETS—National Educational	Examples include but are not limited to:	
Technology Standards; i.e., the	Labs, open-ended essays, voice recordings, videos, presentations, discussion boards, graphic organizers, songs, skits,	
standards for evaluating the skills	dioramas, visual projects (posters, dioramas)	
and knowledge students need to		
learn effectively and live	List the task(s), then explain how the student will demonstrate the transfer of knowledge or skill involved in the task(s)	
productively in an increasingly	(reference Stage 1, Item #4):	
global and digital world.	Student work shared with explanations of work	
	Investigations using Geometric tools, Sketchpad or Desmos to create their own conjectures	
Critical Thinking	Quizzes and tests	
Creative and Innovation	Daily exit tickets	
Communication and Collaboration	Practice proofs	
Technology Operations	Questions regarding daily homework assignments	
	OTHER SUMMATIVE ASSESSMENTS—can include factual recall	
	Examples include but are not limited to final projects, research papers, quizzes and tests.	
	List the assessments:	
	Mid-Unit Quiz	
	End of Unit Quiz	
	Proof Test	

Stage 3 – Learning Plan		
NETS for Students	Learning Activities	Progress Monitoring/Formative Assessment
NETS—National Educational Technology Standards; i.e., the standards for evaluating the skills and knowledge students need to learn effectively and live productively in an increasingly global and digital world.  Communication and Collaboration Creative and Innovation Research and Information Fluency Critical Thinking	<ul> <li>Questions to consider while planning:</li> <li>Are transfer and acquisition addressed in the learning plan?</li> <li>Does the learning plan reflect principles of learning and best practices?</li> <li>Is there tight alignment with Stages 1 and 2?</li> <li>Is the plan likely to be engaging and effective for all students?</li> </ul>	<ul> <li>How will you monitor students' progress toward acquisition, meaning, and transfer during learning activities?         Daily assessments, teacher observation of student inclass performance, teacher observation of student presentations.     </li> <li>What are potential rough spots and student misunderstandings?         Students will have difficulty completing proofs in both equality or congruence situations. Students will struggle calculating missing measures, when the smaller similar triangle is inside the larger corresponding triangle.     </li> </ul>
		<ul> <li>How will students get the feedback they need?</li> </ul>

			Homework assessments, immediate feedback during in-class assignments, mid-chapter quiz, peer feedback and discussion
List pla	nned activities	List resources required	FORMATIVE ASSESSMENTS—any non-graded, diagnostic
(ехатр	les include but are not	(examples include but are not	assessment administered prior to or during a unit that
limited	to: experiments,	limited to: laptops, iPads,	reflects prior knowledge, skill levels, and potential
guided	reading, worksheets,	websites, digital cameras,	misconceptions.
discussi	ions, note-taking,	magazines, Blackboard,	
researc	h, games):	textbooks, novels, primary	Examples include but are not limited to: Pre-tests, clickers
		source documents, other non-	(CPS), mini whiteboards, entrance and exit tickets, CDTs,
Practice	e Proofs	fiction text, lab equipment,	DIBELS, Aimsweb
Peer an	nd Group Proof	maps, translator, calculators)	
practice	9	Textbook, notebook, ruler,	Whiteboards
Experin	nentation	protractor, compass	Warm up problems
Indirect	t Measurement	straightedge, white boards,	Lesson Quizzes
Activity	•	and calculators, sketchpad	Dilation Project
Dilation	n Activity		
Note-ta	aking		
In-Class	s Assignments		

Course: Geometry Unit: Unit 7 - Triangle Applications Grades: 9-10

Stage 1 – Desired Results		
Established Goals	Enduring Understandings/Transfer	
1. What 21 <sup>st</sup> Century Essentials included in	Written as a declarative statement, an enduring understanding is a "big idea" that focuses on larger concepts,	
the mission statement will this unit	principles, and processes that go beyond discrete facts or skills. Enduring Understandings are applicable to	
address?	new situations across content areas and TRANSFERABLE (the ability to learn in one context and apply to a new situation,	
Adaptation and flexibility	particularly outside of the classroom) to the real world.	
Transfer of Learning		
Problem-solving	3. List the Enduring Understanding(s):	
	a. Geometric relationships and concepts can be modeled and applied in areas such as art, architecture,	
2. What content standards will this unit	construction, and engineering.	
address?	b. The modeling of geometric concepts apply in all worldly applications.	
	c. Communication of geometric terms in proper notation and definitions is critical for understanding.	
<ul> <li>ELA PA Core State Standards</li> </ul>	d. Analyze, verify and justify solutions to problems and explain it to others.	
	e. Communicate mathematical concepts to peers, teachers, and instructional assistants in a safe and	
<ul> <li>Math PA Core State Standards</li> </ul>	encouraging environment.	
CC.2.3.HS.A.3: Verify and apply		
geometric theorems as they relate to		
geometric figures.	4. What do you want students to do with this knowledge or skill beyond this course? What is Transfer?	
CC.2.3.HS.A.14: Apply geometric	a. Students will make sense of and persevere in solving complex and novel mathematical problems.	
concepts to model and solve real world	b. Students will use effective mathematical reasoning to construct viable arguments and critique the	
problems.	reasoning of others.	
CC.2.2.HS.C.7 Apply radian measure of an angle and the unit circle to analyze	c. Students will communicate precisely when making mathematical statements and express answers with a degree of precision appropriate for the context of the problem/situation.	
the trigonometric functions.	d. Students will apply mathematical knowledge to analyze and model situations/relationships using multiple	
CC.2.2.HS.C.9 Prove the Pythagorean	representations and appropriate tools in order to make decisions, solve problems, and draw conclusions.	
identity and use it to calculate	e. Students will make use of structure and repeated reasoning to gain a mathematical perspective and	
trigonometric ratios.	formulate generalized problem solving strategies	
PA Content Standards	f. Given a word problem, students will solve the word problem using an appropriate strategy or strategies	
	and will share and compare the use of multiple strategies leading to the same answer.	
	Essential Questions	
	What thought-provoking questions will foster inquiry, meaning-making, and transfer?	

5. List the Essential Question(s) that students should ponder, wonder about or explain by the end of this unit: In what ways can triangles be applied in the real world: engineering, construction, etc?

## Acquisition

## Students will know...

- 6. What facts should students know and be able to use to gain further knowledge?

  Difference between a leg and the hypotenuse Applying the Pythagorean Theorem

  Notation of special right triangles

  Applying the basic trigonometric functions
  (SOHCAHTOA)

  Applying angles of elevation and depression
  Solving for missing lengths and angles
- 7. What vocabulary should students know and be able to recall?
  Right triangle, obtuse triangle, acute triangle,
  Pythagorean Theorem, legs, hypotenuse, isosceles right triangles, 30/60/90 triangles sin, cos, tan,
  SOHCAHTOA, theta, angle of elevation, angle of depression, Law of Sines, Law of Cosines, Unit Circle
- 8. What basic concepts should students know and be able to recall and apply?

  Students will apply the Pythagorean Theorem to solve for legs or the hypotenuse of a right triangle.

  Students will use the shortcuts to determine missing lengths in special right triangles

  Students will use the basic trigonometric functions to determine missing angles or sides in right triangles

  Students will apply angles of elevation and angles of depression to real life situations

  Students will apply the Law of Sines or the Law of Cosines to triangles that are not right triangles

  Students will apply special right triangles to the Unit Circle

## Students will be skilled at... (be able to do)

- 9. What discrete skill and processes should students be able to demonstrate?
  - *G.1.2.1.1* Identify and/or use properties of triangles
  - G.1.2.1.3 Identify and/or use properties of isosceles and equilateral triangles.
  - G.1.3.2.1 Write, analyze, complete, or identify formal proofs (e.g., direct and/or indirect proofs/proofs by contradiction)
  - G.2.1.1.1 Use the Pythagorean Theorem to write and/or solve problems involving right triangles.
    G.2.1.1.2 Use trigonometric ratios to write and/or solve problems involving right triangles.
    G.2.1.2.1 Calculate the distance and/or midpoint between two points on a number line or on a coordinate plane

#### G.2.2.3.1

Describe how a change in the linear dimension of a figure affects its perimeter, circumference, and area

Stage 2 – Evidence			
NETS for Students	PERFORMANCE TASK(S)—can include transfer tasks and Project-Based Learning		
NETS—National Educational	Examples include but are not limited to:		
Technology Standards; i.e., the	Labs, open-ended essays, voice recordings, videos, presentations, discussion boards, graphic organizers, songs, skits,		
standards for evaluating the skills	dioramas, visual projects (posters, dioramas)		
and knowledge students need to			
learn effectively and live	List the task(s), then explain how the student will demonstrate the transfer of knowledge or skill involved in the task(s)		
productively in an increasingly	(reference Stage 1, Item #4):		
global and digital world.	Student work shared with explanations of work and comparisons to other solutions		
	Investigations using Geometric tools, Sketchpad or Desmos to create their own conjectures		
Critical Thinking	Peer reviewed work		
Creative and Innovation	Quizzes and tests		
	Daily exit tickets		
	Collection/grading of daily homework assignments		
	OTHER SUMMATIVE ASSESSMENTS—can include factual recall		
	Examples include but are not limited to final projects, research papers, quizzes and tests.		
	List the assessments:		
	Mid-Unit Quiz		
	Unit 6 Exam		

Stage 3 – Learning Plan			
NETS for Students	Learning Activities	Progress Monitoring/Formative Assessment	
NETS—National Educational Technology Standards; i.e., the standards for evaluating the skills and knowledge students need to learn effectively and live productively in an increasingly global and digital world.  Communication and Collaboration Creative and Innovation	<ul> <li>Questions to consider while planning:</li> <li>Are transfer and acquisition addressed in the learning plan?</li> <li>Does the learning plan reflect principles of learning and best practices?</li> <li>Is there tight alignment with Stages 1 and 2?</li> <li>Is the plan likely to be engaging and effective for all students?</li> </ul>	<ul> <li>How will you monitor students' progress toward acquisition, meaning, and transfer during learning activities?         Daily assessments, teacher observation of student inclass performance, teacher observation of student presentations.     </li> <li>What are potential rough spots and student misunderstandings?         Appropriately determining the proper trigonometric functions or rules for determining missing pieces of     </li> </ul>	
Research and Information Fluency Critical Thinking		<ul> <li>How will students get the feedback they need?</li> <li>Graded homework assessments, immediate feedback during in-class assignments, mid-chapter quiz, peer feedback and discussion</li> </ul>	

Lis	st planned activities	List resources required	FORMATIVE ASSESSMENTS—any non-graded, diagnostic
(ex	xamples include but are not	(examples include but are not	assessment administered prior to or during a unit that
lim	mited to: experiments,	limited to: laptops, iPads,	reflects prior knowledge, skill levels, and potential
gu	uided reading, worksheets,	websites, digital cameras,	misconceptions.
dis	scussions, note-taking,	magazines, Blackboard,	
res	esearch, games):	textbooks, novels, primary	Examples include but are not limited to: Pre-tests, clickers
		source documents, other non-	(CPS), mini whiteboards, entrance and exit tickets, CDTs,
		fiction text, lab equipment,	DIBELS, Aimsweb
Py	ythagorean Pictionary	maps, translator, calculators)	
De	efinition Presentations	Textbook, notebook, ruler,	Whiteboards
We	ord Wall	protractor, compass	Warm up problems
No	ote-taking	straightedge, white boards,	
In-	-Class Assignments	and calculators	



Date: October, 2016

Course: Geometry Unit: Unit 8 - Circles Grades: 9-10

Teacher Team: Greenawald, Dottery, Skrapits, Everett

Stage 1 – Desired Results		
Established Goals	Enduring Understandings/Transfer	
1. What 21 <sup>st</sup> Century Essentials included in the mission statement will this unit	Written as a declarative statement, an enduring understanding is a "big idea" that focuses on larger concepts, principles, and processes that go beyond discrete facts or skills. Enduring Understandings are applicable to	
address?  Adaptation and flexibility  Transfer of Learning	new situations across content areas and <a href="TRANSFERABLE">TRANSFERABLE</a> (the ability to learn in one context and apply to a new situation, particularly outside of the classroom) to the real world.	
Problem-solving Effective Communication Skills	3. List the Enduring Understanding(s):  a. Geometric relationships and concepts can be modeled and applied in areas such as art, architecture, construction, and engineering.	
2. What content standards will this unit address?	b. Inductive and deductive reasoning skills can be applied through geometric concepts and results in drawing reasonable conclusions.	
• ELA PA Core State Standards	<ul> <li>c. The modeling of geometric concepts apply in all worldly applications.</li> <li>d. Communication of geometric terms in proper notation and definitions is critical for understanding.</li> <li>e. Students analyze, verify and justify their solutions to problems and can explain it to others.</li> </ul>	
<ul> <li>Math PA Core State Standards         CC.2.3.HS.A.3: Verify and apply geometric theorems as they relate to geometric figures.     </li> </ul>	f. Communicate mathematical concepts to peers, teachers, and instructional assistants in a safe and encouraging environment.	
CC.2.3.HS.A.14: Apply geometric concepts to model and solve real world problems. CC.2.3.HS.A.8 Apply theorems to verify	<ul> <li>4. What do you want students to do with this knowledge or skill beyond this course? What is Transfer?</li> <li>a. Students will make sense of and persevere in solving complex and novel mathematical problems.</li> <li>b. Students will use effective mathematical reasoning to construct viable arguments and critique the reasoning of others.</li> </ul>	
properties of circles.  • PA Content Standards	c. Students will communicate precisely when making mathematical statements and express answers with a degree of precision appropriate for the context of the problem/situation.	
	<ul> <li>d. Students will apply mathematical knowledge to analyze and model situations/relationships using multiple representations and appropriate tools in order to make decisions, solve problems, and draw conclusions.</li> <li>e. Students will make use of structure and repeated reasoning to gain a mathematical perspective and formulate generalized problem solving strategies</li> <li>f. Given a word problem, students will solve the word problem using an appropriate strategy or strategies and will share and compare the use of multiple strategies leading to the same answer.</li> </ul>	

## What thought-provoking questions will foster inquiry, meaning-making, and transfer?

5. List the Essential Question(s) that students should ponder, wonder about or explain by the end of this unit: How do the relationships of angles and segments that intersect with circles help us solve real-world problems?

## Acquisition

#### Students will know...

- 6. What facts should students know and be able to use to gain further knowledge?

  Proper Geometry notation

  Properties of Similar Triangles

  Area and perimeter formulas for circles

  How to prove similarity in triangles
- 7. What vocabulary should students know and be able to recall?

  adjacent arcs, arc, arc length, central angle, chord, common tangent, concentric circles, congruent arcs, congruent circles, exterior of a circle, inscribed angle, intercepted arc, interior of a circle, major arc, minor arc, point of tangency, secant, sector of a circle, semicircle, tangent
- 8. What basic concepts should students know and be able to recall and apply?

  Identify and describe relationships among inscribed angles, radii and chords.

  Apply properties of arcs and chords.

  Find the area of sectors and lengths of arcs

  Find the measure of inscribed angles, central angles, and measures of angles formed by lines that intersect circles.

  Find the lengths of segments formed by lines that intersect circles.

Write equations and graph circles to solve problems.

- 9. What discrete skill and processes should students be able to demonstrate?
  - G.1.1.1.1 Identify, determine, and/or use the radius, diameter, segment, and/or tangent of a circle.
    G.1.1.1.2 Identify, determine, and/or use the arcs, semicircles, sectors, and/or angles of a circle.
    G.1.1.1.3 Use chords, tangents, and secants to find missing arc measures or missing segment measures.
  - G.1.2.1.1 Identify and/or use properties of triangles G.1.2.1.2 Identify and/or use properties of quadrilaterals
  - G.1.2.1.3 Identify and/or use properties of isosceles and equilateral triangles.
  - G.1.2.1.4 Identify and/or use properties of regular polygons
  - G.1.3.1.1 Identify and/or use properties of congruent and similar polygons or solids. G.1.3.1.2 Identify and/or use proportional relationships in similar figures.
  - G.2.1.1.1 Use the Pythagorean Theorem to write and/or solve problems involving right triangles.
  - G.2.2.2.5 Find the area of a sector of a circle.
  - G.1.3.2.1 Write, analyze, complete or identify formal proofs.

	G.2.2.1.1 Use properties of angles formed by intersecting lines to find the measures of missing angles. G.2.2.1.2 Use properties of angles formed when two parallel lines are cut by a transversal to find the measures of missing angles.
	G.2.2.3.1  Describe how a change in the linear dimension of a figure affects its perimeter, circumference, and area

Stage 2 – Evidence			
NETS for Students	PERFORMANCE TASK(S)—can include transfer tasks and Project-Based Learning		
NETS—National Educational	Examples include but are not limited to:		
Technology Standards; i.e., the	Labs, open-ended essays, voice recordings, videos, presentations, discussion boards, graphic organizers, songs, skits,		
standards for evaluating the skills	dioramas, visual projects (posters, dioramas)		
and knowledge students need to			
learn effectively and live	List the task(s), then explain how the student will demonstrate the transfer of knowledge or skill involved in the task(s)		
productively in an increasingly	(reference Stage 1, Item #4):		
global and digital world.	Student work shared with explanations of work		
	Investigations using Geometric tools, Sketchpad or Desmos to create their own conjectures		
Critical Thinking	Peer reviewed work - Angle Puzzles		
Creative and Innovation	Peer reviewed work - Segment Problems		
Communication and Collaboration	Quizzes and tests		
Technology Operations	Daily exit tickets		
	Questions regarding daily homework assignments		
	OTHER SUMMATIVE ASSESSMENTS—can include factual recall		
	Examples include but are not limited to final projects, research papers, quizzes and tests.		
	List the assessments:		
	Mid-Unit Quiz		
	End of Unit Quiz		

Stage 3 – Learning Plan				
NETS for Students	Learning Activities		Progress Monitoring/Formative Assessment	
NETS—National Educational Technology Standards; i.e., the standards for evaluating the skills and knowledge students need to learn effectively and live productively in an increasingly global and digital world.  Communication and Collaboration Creative and Innovation Research and Information Fluency Critical Thinking	Questions to consider while planning:  • Are transfer and acquisition addressed in the learning		<ul> <li>How will you monitor students' progress toward acquisition, meaning, and transfer during learning activities?         Daily assessments, teacher observation of student inclass performance, teacher observation of student presentations.     </li> <li>What are potential rough spots and student misunderstandings?         Students will have difficulty with the quantity of equations to remember. Segments in circles give students the most difficulty when applying the algebra.     </li> </ul>	
	List planned activities (examples include but are not limited to: experiments, guided reading, worksheets, discussions, note-taking, research, games):  Student-created Angle Puzzles Student-created Segment problems Note-taking In-Class Assignments	List resources required (examples include but are not limited to: laptops, iPads, websites, digital cameras, magazines, Blackboard, textbooks, novels, primary source documents, other non- fiction text, lab equipment, maps, translator, calculators) Textbook, notebook, ruler, protractor, compass straightedge, white boards, and calculators, sketchpad	How will students get the feedback they need?     Homework assessments, immediate feedback during in-class assignments, mid-chapter quiz, peer feedback and discussion  FORMATIVE ASSESSMENTS—any non-graded, diagnostic assessment administered prior to or during a unit that reflects prior knowledge, skill levels, and potential misconceptions.  Examples include but are not limited to: Pre-tests, clickers (CPS), mini whiteboards, entrance and exit tickets, CDTs, DIBELS, Aimsweb  Whiteboards Warm up problems Lesson Quizzes	



Course: Geometry Unit: Unit 9 - Area of Polygons/Polyhedrons Grades: 9-10

Stage 1 – Desired Results		
<b>Established Goals</b>	Enduring Understandings/Transfer	
1. What 21 <sup>st</sup> Century Essentials included in	Written as a declarative statement, an enduring understanding is a "big idea" that focuses on larger concepts,	
the mission statement will this unit	principles, and processes that go beyond discrete facts or skills. Enduring Understandings are applicable to	
address?	new situations across content areas and TRANSFERABLE (the ability to learn in one context and apply to a new situation,	
Adaptation and flexibility	particularly outside of the classroom) to the real world.	
Transfer of Learning		
Problem-solving	3. List the Enduring Understanding(s):	
	a. Geometric relationships and concepts can be modeled and applied in areas such as art, architecture,	
2. What content standards will this unit	construction, and engineering.	
address?	b. Inductive and deductive reasoning skills can be applied through geometric concepts and results in drawing reasonable conclusions.	
• ELA PA Core State Standards	c. The modeling of geometric concepts apply in all worldly applications.	
	d. Communication of geometric terms in proper notation and definitions is critical for understanding.	
<ul> <li>Math PA Core State Standards</li> </ul>	e. Analyze, verify and justify solutions to problems and explain it to others.	
CC.2.3.HS.A.3: Verify and apply	f. Communicate mathematical concepts to peers, teachers, and instructional assistants in a safe and	
geometric theorems as they relate to	encouraging environment.	
geometric figures.	g. Area of polygons and surface area of polyhedrons are critical in solving real world problems and situations.	
CC.2.3.HS.A.14: Apply geometric		
concepts to model and solve real world problems.	4. What do you want students to do with this knowledge or skill beyond this course? What is Transfer?	
PA Content Standards	a. Students will make sense of and persevere in solving complex and novel mathematical problems.	
PA Content Standards	<ul> <li>b. Students will use effective mathematical reasoning to construct viable arguments and critique the reasoning of others.</li> </ul>	
	c. Students will communicate precisely when making mathematical statements and express answers with a degree of precision appropriate for the context of the problem/situation.	
	<ul> <li>d. Students will apply mathematical knowledge to analyze and model situations/relationships using multiple representations and appropriate tools in order to make decisions, solve problems, and draw conclusions.</li> <li>e. Students will make use of structure and repeated reasoning to gain a mathematical perspective and formulate generalized problem solving strategies</li> </ul>	
	f. Given a word problem, students will solve the word problem using an appropriate strategy or strategies and will share and compare the use of multiple strategies leading to the same answer.	

## What thought-provoking questions will foster inquiry, meaning-making, and transfer?

5. List the Essential Question(s) that students should ponder, wonder about or explain by the end of this unit: How do I determine surface area of various polygons and polyhedrons and how are these skills applied to real world problems?

### **Acquisition**

#### Students will know...

- 6. What facts should students know and be able to use to gain further knowledge?

  Concept of area and square units

  Classifying polygons and polyhedrons

  Solving for a single variable using algebra
- 7. What vocabulary should students know and be able to recall?

  Rectangle, parallelogram, triangle, kite, trapezoid, regular polygon, apothem, side length, equilateral, isosceles, diagonal, base, altitude (height), circle, sector of a circle, segment of a circle, annulus, cone, sphere, pyramid, cylinder, prism
- 8. What basic concepts should students know and be able to recall and apply?

  Determine the type of polygon or polyhedron.

  Apply the corresponding area formula to the polygon or polyhedron.

  Use basic algebraic skills to solve for missing variables.

  Apply the formula to the real world application.

- 9. What discrete skill and processes should students be able to demonstrate?
  - G.1.1.1.1 Identify, determine, and/or use the radius, diameter, segment, and/or tangent of a circle G.1.1.1.2 Identify, determine, and/or use the arcs, semicircles, sectors, and/or angles of a circle G.1.1.1.4 Identify and/or use the properties of a sphere or cylinder
  - G.1.2.1.1 Identify and/or use properties of triangles G.1.2.1.2 Identify and/or use properties of auadrilaterals
  - G.1.2.1.3 Identify and/or use properties of isosceles and equilateral triangles.
  - G.1.2.1.4 Identify and/or use properties of regular polygons
  - G.1.2.1.5 Identify and/or use properties of pyramids and prisms
  - G.2.1.1.1 Use the Pythagorean Theorem to write and/or solve problems involving right triangles.
  - G.2.2.2.1 Estimate area, perimeter, or circumference of an irregular figure.
  - G.2.2.2.2 Find the measurement of a missing length, given the perimeter, circumference, or area.
  - G.2.2.2.3 Find the side lengths of a polygon with a given perimeter to maximize the area of the polygon G.2.2.2.4 Develop and/or use strategies to estimate

the area of a compound/composite figure G.2.2.3.1 Describe how a change in the linear dimension of a figure affects its perimeter, circumference, and area G.2.2.4.1 Use area models to find probabilities
G.2.3.2.1 Describe how a change in the linear dimension of a figure affects its surface area or volume G.2.3.1.1 Calculate the surface area of prisms, cylinders, cones, pyramids, and/or spheres G.2.3.1.3 Find the measurement of a missing lengt given the surface area or volume

	Stage 2 – Evidence
NETS for Students	PERFORMANCE TASK(S)—can include transfer tasks and Project-Based Learning
NETS—National Educational	Examples include but are not limited to:
Technology Standards; i.e., the	Labs, open-ended essays, voice recordings, videos, presentations, discussion boards, graphic organizers, songs, skits,
standards for evaluating the skills	dioramas, visual projects (posters, dioramas)
and knowledge students need to	
learn effectively and live	List the task(s), then explain how the student will demonstrate the transfer of knowledge or skill involved in the task(s)
productively in an increasingly	(reference Stage 1, Item #4):
global and digital world.	Student work shared with explanations of work and comparisons to other solutions
	Investigations using Geometric tools, Sketchpad or Desmos to create their own conjectures
Critical Thinking	Peer reviewed work
Creative and Innovation	Quizzes and tests
	Daily exit tickets
	Collection/grading of daily homework assignments
	OTHER SUMMATIVE ASSESSMENTS—can include factual recall
	Examples include but are not limited to final projects, research papers, quizzes and tests.
	List the assessments:
	Mid-Unit Quiz
	Unit 9 Test

# Stage 3 – Learning Plan

NETS for Students	Learning Activities		Progress Monitoring/Formative Assessment
NETS—National Educational Technology Standards; i.e., the standards for evaluating the skills and knowledge students need to learn effectively and live productively in an increasingly global and digital world.  Communication and Collaboration Creative and Innovation Research and Information Fluency Critical Thinking	<ul> <li>Questions to consider while plae</li> <li>Are transfer and acquisition plan?</li> <li>Does the learning plan reflee best practices?</li> <li>Is there tight alignment with list the plan likely to be engaged students?</li> </ul>	anning: n addressed in the learning ect principles of learning and th Stages 1 and 2?	<ul> <li>How will you monitor students' progress toward acquisition, meaning, and transfer during learning activities?         Daily assessments, teacher observation of student inclass performance, teacher observation of student presentations.     </li> <li>What are potential rough spots and student misunderstandings?         Determining the 2 or 3 dimensional shape and it's appropriate formula.         Solving for missing lengths, sides, etc. using algebra.     </li> <li>How will students get the feedback they need?         Graded homework assessments, immediate feedback during in-class assignments, mid-chapter quiz, peer feedback and discussion     </li> </ul>
	List planned activities (examples include but are not limited to: experiments, guided reading, worksheets, discussions, note-taking, research, games):  Area Investigations Definition Presentations Word Wall Note-taking In-Class Assignments	List resources required (examples include but are not limited to: laptops, iPads, websites, digital cameras, magazines, Blackboard, textbooks, novels, primary source documents, other nonfiction text, lab equipment, maps, translator, calculators)  Textbook, notebook, ruler, protractor, compass straightedge, white boards, and calculators	FORMATIVE ASSESSMENTS—any non-graded, diagnostic assessment administered prior to or during a unit that reflects prior knowledge, skill levels, and potential misconceptions.  Examples include but are not limited to: Pre-tests, clickers (CPS), mini whiteboards, entrance and exit tickets, CDTs, DIBELS, Aimsweb  Whiteboards Warm up problems



Course: Geometry Unit: Unit 10 - Volume Grades: 9-10

	Stage 1 – Desired Results
Established Goals	Enduring Understandings/Transfer
What 21 <sup>st</sup> Century Essentials included in the mission statement will this unit address?      Adaptation and flexibility      Transfer of Learning	Written as a declarative statement, an enduring understanding is a "big idea" that focuses on larger concepts, principles, and processes that go beyond discrete facts or skills. Enduring Understandings are applicable to new situations across content areas and <a href="https://example.com/real-world-new-situation">TRANSFERABLE</a> (the ability to learn in one context and apply to a new situation, particularly outside of the classroom) to the real world.
Problem-solving	3. List the Enduring Understanding(s):  a. Geometric relationships and concepts can be modeled and applied in areas such as art, architecture,
2. What content standards will this unit address?	construction, and engineering. b. Inductive and deductive reasoning skills can be applied through geometric concepts and results in drawing reasonable conclusions.
ELA PA Core State Standards     Nath DA Core State Standards	c. The modeling of geometric concepts apply in all worldly applications. d. Communication of geometric terms in proper notation and definitions is critical for understanding.
<ul> <li>Math PA Core State Standards         CC.2.3.HS.A.3: Verify and apply             geometric theorems as they relate to             geometric figures.         CC.2.3.HS.A.12 Explain volume formulas             and use them to solve problems.     </li> </ul>	<ul> <li>e. Analyze, verify and justify solutions to problems and explain it to others.</li> <li>f. Communicate mathematical concepts to peers, teachers, and instructional assistants in a safe and encouraging environment.</li> <li>g. Volume of 3 dimensional objects are critical in solving real world problems and situations.</li> </ul>
CC.2.3.HS.A.14: Apply geometric concepts to model and solve real world problems.  • PA Content Standards	<ul> <li>4. What do you want students to do with this knowledge or skill beyond this course? What is Transfer?</li> <li>a. Students will make sense of and persevere in solving complex and novel mathematical problems.</li> <li>b. Students will use effective mathematical reasoning to construct viable arguments and critique the reasoning of others.</li> <li>c. Students will communicate precisely when making mathematical statements and express answers with a degree of precision appropriate for the context of the problem/situation.</li> </ul>
	d. Students will apply mathematical knowledge to analyze and model situations/relationships using multiple representations and appropriate tools in order to make decisions, solve problems, and draw conclusions.  e. Students will make use of structure and repeated reasoning to gain a mathematical perspective and formulate generalized problem solving strategies  f. Given a word problem, students will solve the word problem using an appropriate strategy or strategies and will share and compare the use of multiple strategies leading to the same answer.

## What thought-provoking questions will foster inquiry, meaning making, and transfer?

5. List the Essential Question(s) that students should ponder, wonder about or explain by the end of this unit: How do I determine volume of various 3 dimensional solids and how are these skills applied to real world problems?

## Acquisition

### Students will know...

- 6. What facts should students know and be able to use to gain further knowledge?

  Concept of volume and cubic units

  Classifying 3 dimensional solids

  Solving for a single variable using algebra
- 7. What vocabulary should students know and be able to recall?

  Rectangle, parallelogram, triangle, kite, trapezoid, regular polygon, apothem, side length, equilateral, isosceles, diagonal, base, altitude (height), circle, sector of a circle, segment of a circle, annulus, cone, sphere, hemisphere, pyramid, cylinder, prism, polyhedron, edge, face, vertex, lateral, oblique
- 8. What basic concepts should students know and be able to recall and apply?

  Determine the type of polyhedron

  Apply the corresponding volume formula to the 3 dimensional solid

  Use basic algebraic skills to solve for missing variables

  Apply the formula to the real world application.

- 9. What discrete skill and processes should students be able to demonstrate?
  - G.1.1.1.1 Identify, determine, and/or use the radius, diameter, segment, and/or tangent of a circle G.1.1.1.2 Identify, determine, and/or use the arcs, semicircles, sectors, and/or angles of a circle G.1.1.1.4 Identify and/or use the properties of a sphere or cylinder
  - G.1.2.1.1 Identify and/or use properties of triangles G.1.2.1.2 Identify and/or use properties of quadrilaterals
  - G.1.2.1.3 Identify and/or use properties of isosceles and equilateral triangles.
  - G.1.2.1.4 Identify and/or use properties of regular polygons
  - G.1.2.1.5 Identify and/or use properties of pyramids and prisms
  - G.2.1.1.1 Use the Pythagorean Theorem to write and/or solve problems involving right triangles.
  - G.2.2.3.1 Describe how a change in the linear dimension of a figure affects its perimeter, circumference, and area

	G.2.3.1.1 Calculate the surface area of prisms, cylinders, cones, pyramids, and/or spheres G.2.3.1.2 Calculate the volume of prisms, cylinders, cones, pyramids, and/or spheres G.2.3.1.3 Find the measurement of a missing length given the surface area or volume
	G.2.3.2.1 Describe how a change in the linear dimension of a figure affects its surface area or volume

	Stage 2 – Evidence
NETS for Students	PERFORMANCE TASK(S)—can include transfer tasks and Project-Based Learning
NETS—National Educational	Examples include but are not limited to:
Technology Standards; i.e., the	Labs, open-ended essays, voice recordings, videos, presentations, discussion boards, graphic organizers, songs, skits,
standards for evaluating the skills	dioramas, visual projects (posters, dioramas)
and knowledge students need to	
learn effectively and live	List the task(s), then explain how the student will demonstrate the transfer of knowledge or skill involved in the task(s)
productively in an increasingly	(reference Stage 1, Item #4):
global and digital world.	Student work shared with explanations of work and comparisons to other solutions
	Investigations using Geometric tools, Sketchpad or Desmos to create their own conjectures
Critical Thinking	Peer reviewed work
Creative and Innovation	Quizzes and tests
	Daily exit tickets
	Collection/grading of daily homework assignments
	OTHER SUMMATIVE ASSESSMENTS—can include factual recall
	Examples include but are not limited to final projects, research papers, quizzes and tests.
	List the assessments:
	Mid-Unit Quiz
	Unit 10 Test

	Stage 3 – Learning Plan	
NETS for Students	Learning Activities	Progress Monitoring/Formative Assessment

NETS—National Educational
Technology Standards; i.e., the
standards for evaluating the skills
and knowledge students need to
learn effectively and live
productively in an increasingly
global and digital world.

Communication and Collaboration Creative and Innovation Research and Information Fluency Critical Thinking

Questions to consider while planning:

- Are transfer and acquisition addressed in the learning plan?
- Does the learning plan reflect principles of learning and best practices?
- Is there tight alignment with Stages 1 and 2?
- Is the plan likely to be engaging and effective for all students?

• How will you monitor students' progress toward acquisition, meaning, and transfer during learning activities?

Daily assessments, teacher observation of student inclass performance, teacher observation of student presentations.

 What are potential rough spots and student misunderstandings?

Applying area formulas appropriately and applying them to their respective needs in determining volume.

Algebraically solving for missing variables or lengths.

• How will students get the feedback they need? Graded homework assessments, immediate feedback during in-class assignments, mid-chapter quiz, peer feedback and discussion

List planned activities

(examples include but are not limited to: experiments, guided reading, worksheets, discussions, note-taking, research, games):

**Volume Investigations Definition Presentations** Word Wall Note-taking **In-Class Assignments** 

List resources required

(examples include but are not limited to: laptops, iPads, websites, digital cameras, magazines, Blackboard, textbooks, novels, primary source documents, other nonfiction text, lab equipment, maps, translator, calculators)

Textbook, notebook, ruler, protractor, compass straightedge, white boards, and calculators

FORMATIVE ASSESSMENTS—any non-graded, diagnostic assessment administered prior to or during a unit that reflects prior knowledge, skill levels, and potential misconceptions.

Examples include but are not limited to: Pre-tests, clickers (CPS), mini whiteboards, entrance and exit tickets, CDTs, DIBELS, Aimsweb

Whiteboards Warm up problems